The Area Between Curves

1. Find the area bounded by the given curve and the $x$-axis.

$$
y=x^{4}-4 x^{3}
$$


2. Find the area bounded by the given curve and the $x$-axis on the interval $[-10,10]$.
$y=\frac{2 x}{x^{2}+6}$

3. Find the area bounded by the given curves.

$$
y=x^{3}, y=x+6, y=-\frac{1}{2} x
$$


4. Find the area of the region bounded below by the given curve and above by the $x$-axis from $x=0$ to $x=1$.

$$
y=-x \cdot e^{-x^{2}}
$$


5. Sketch the graphs of $f$ and $g$ and find the area of the region enclosed by these graphs and the vertical lines $x=-2$ to $x=1$.
$f(x)=x+2$ and $g(x)=x^{2}-4$
6. Sketch the graphs of $f$ and $g$ and find the area of the region enclosed by these graphs where $x \geq 0$.
$f(x)=x-2$ and $g(x)=\sqrt{x}$
7. Sketch the graph of $f(x)=x^{3}$ and find the area of the region bounded below by the graph of $f(x)$ and above by the $x$-axis from $x=-5$ to $x=0$.
8. Sketch the graphs of $f(x)=x^{2}+2$ and $g(x)=1$.

Find the area of the region enclosed by these graphs and the vertical lines $x=3$ and $x=5$.
9. Sketch the graphs of $f(x)=-x^{2}+2 x+1$ and $g(x)=-x+1$.

Find the area of the region enclosed by these graphs and the vertical lines $x=0$ and $x=1$.

